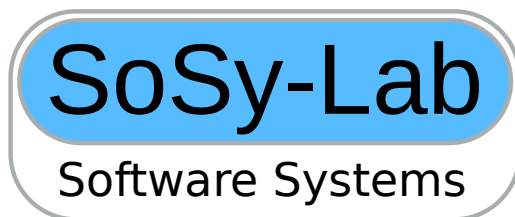
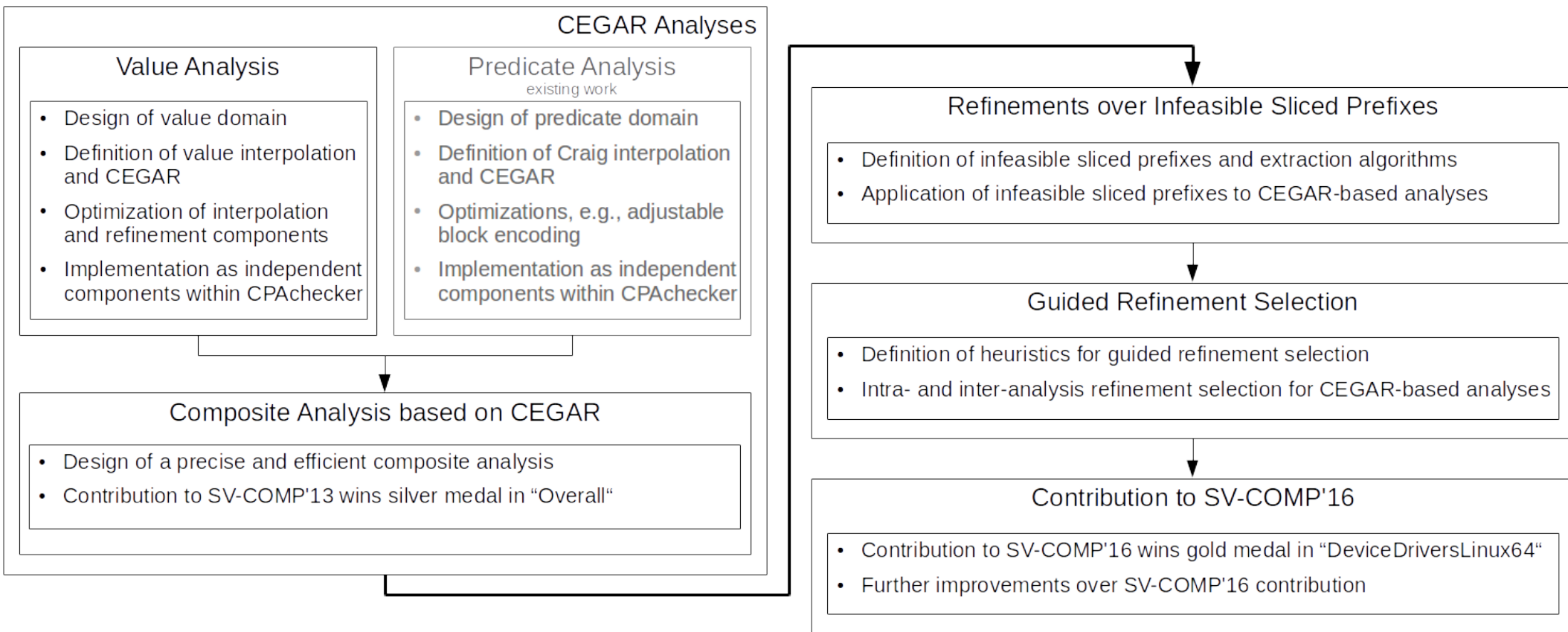


# Effective Approaches to Abstraction Refinement for an Explicit Value Analysis

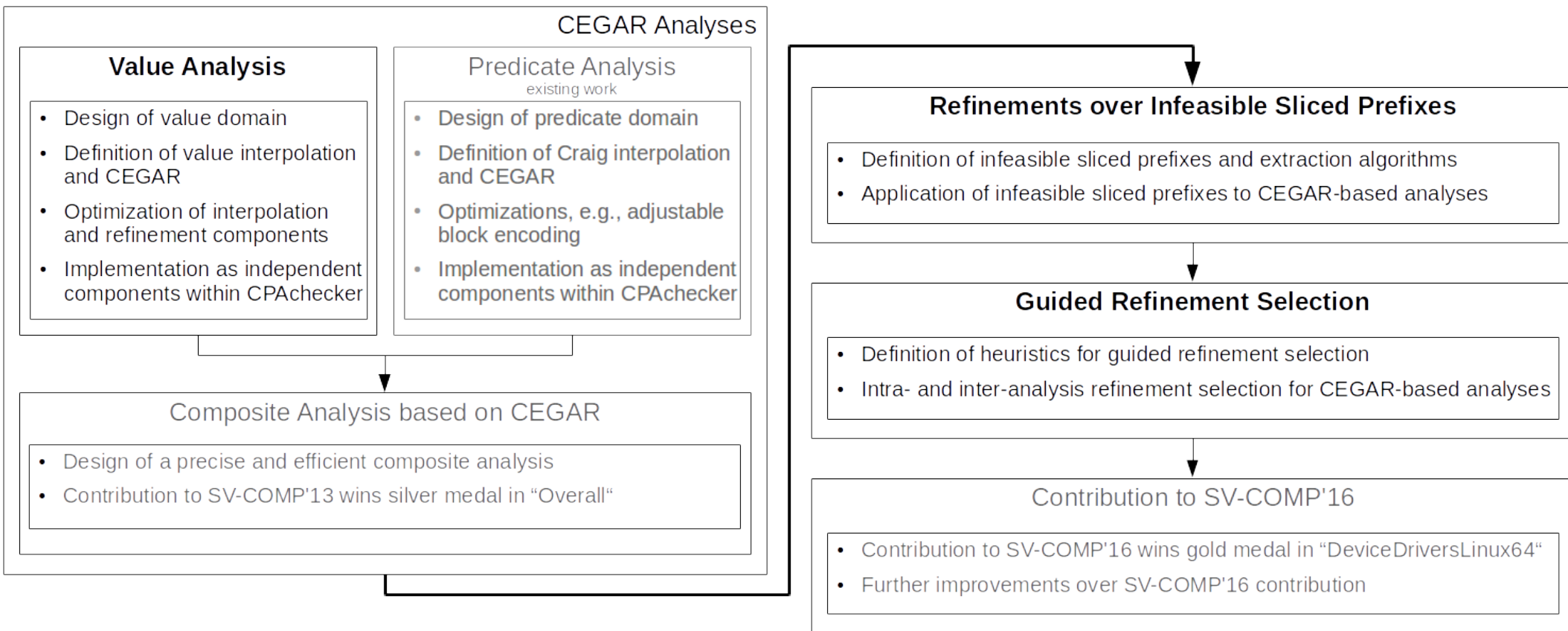
Stefan Löwe



# Outline of my Thesis

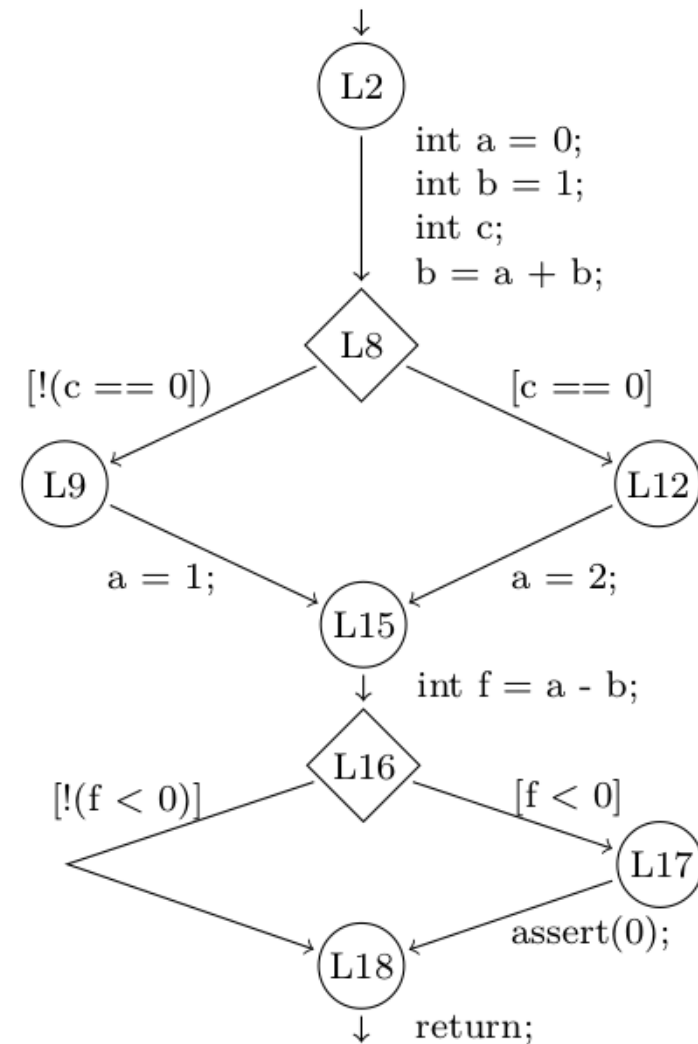


# Outline of my Talk



# Value Analysis by Example

```
1 #include <assert.h>
2 int main() {
3     int a = 0;
4     int b = 1;
5     int c;
6     b = a + b;
7
8     if (c) {
9         a = 1;
10    }
11    else {
12        a = 2;
13    }
14
15    int f = a - b;
16    if (f < 0) {
17        assert(0);
18    }
19 }
```

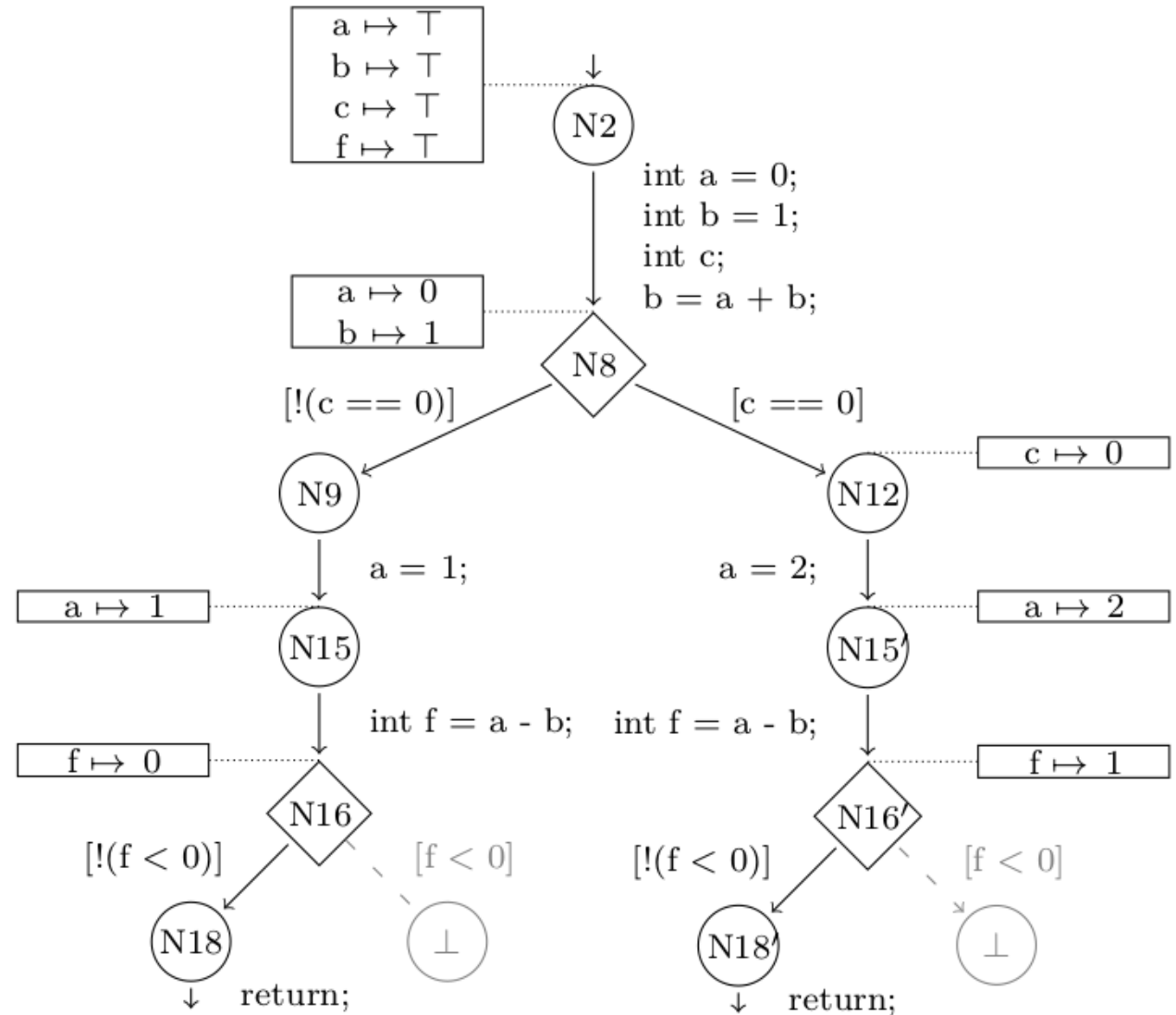


# Value Analysis by Example

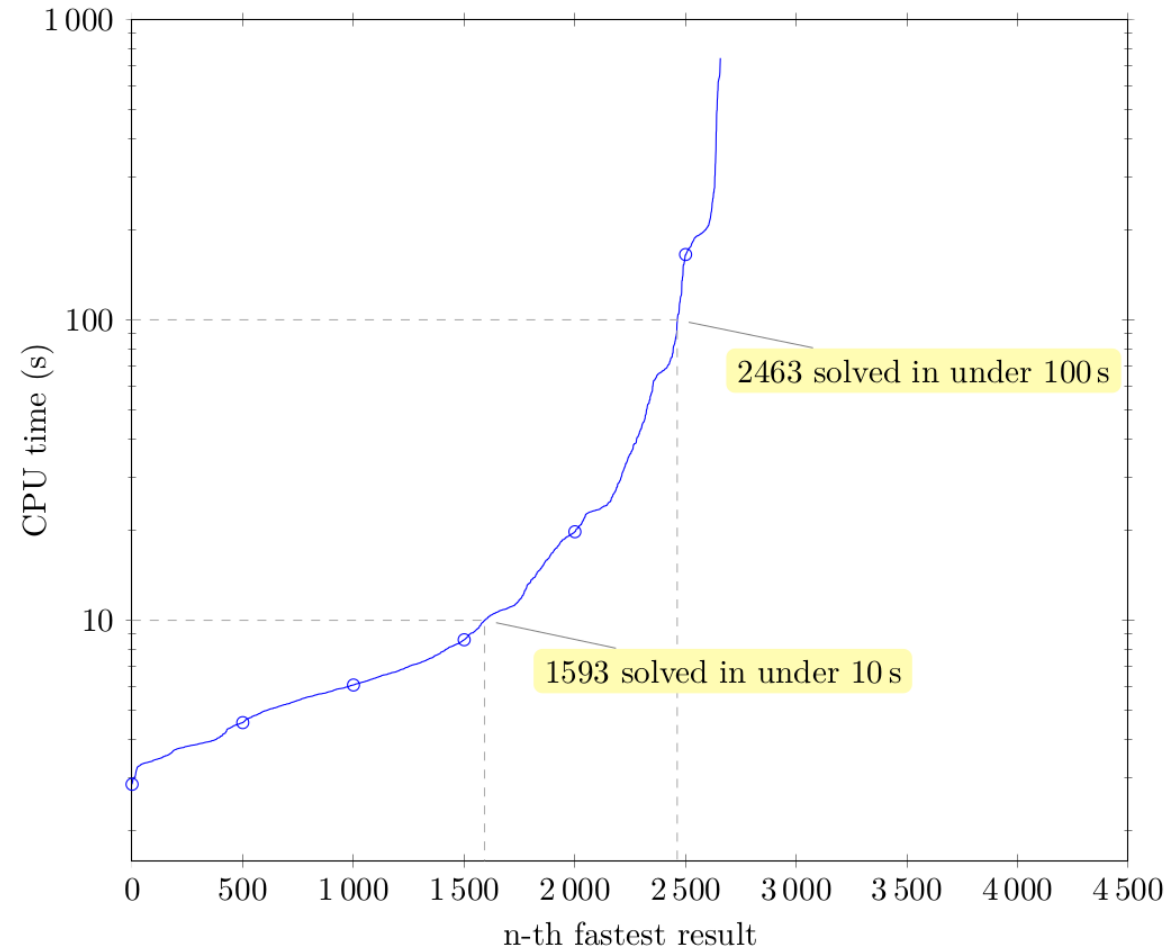
```

1 #include <assert.h>
2 int main() {
3     int a = 0;
4     int b = 1;
5     int c;
6     b = a + b;
7
8     if (c) {
9         a = 1;
10    }
11    else {
12        a = 2;
13    }
14
15    int f = a - b;
16    if (f < 0) {
17        assert(0);
18    }
19 }

```



# Value Analysis by the Numbers

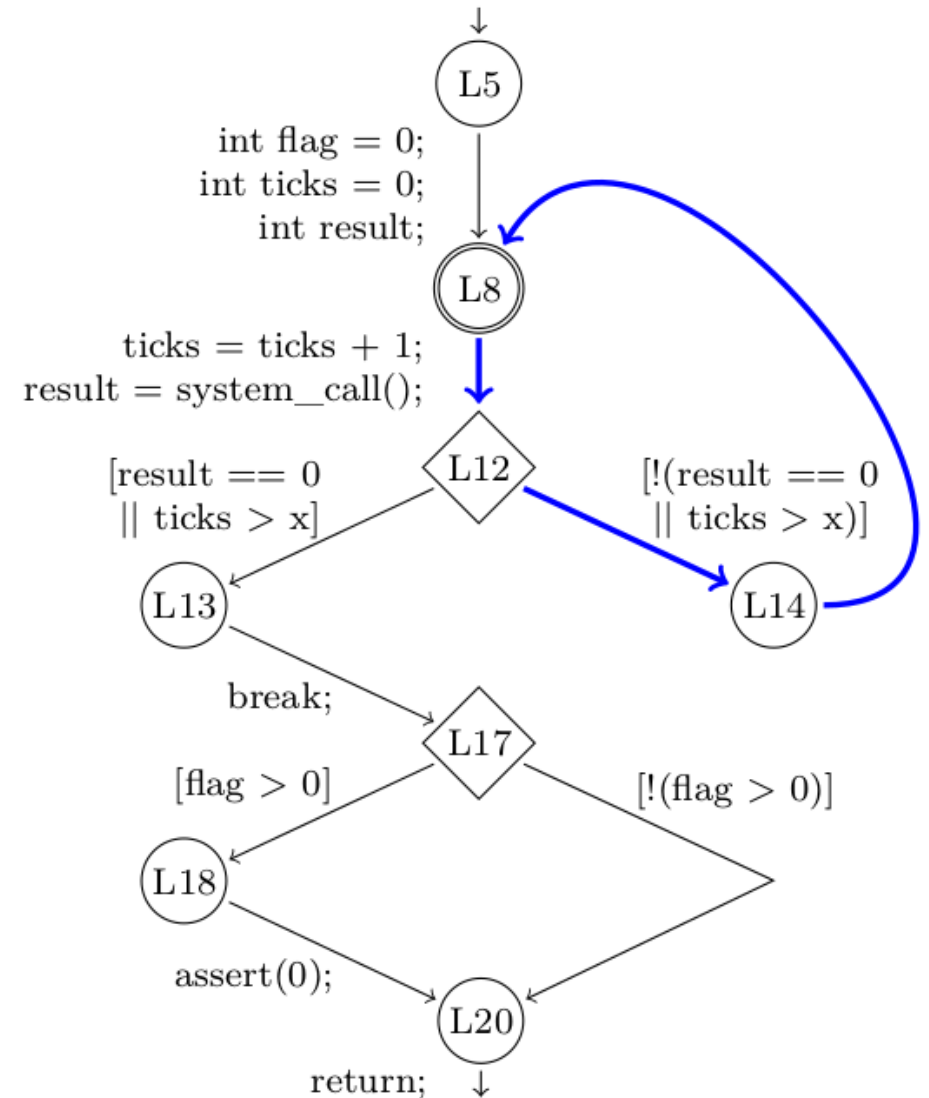


- Well over 4000 verification tasks from SV-COMP'16
- **VA solves almost two thirds**
- Under SV-COMP'16 rules, complete evaluation takes 440 hours
- 410 hours, or 93%, are **wasted** for unsolved verification tasks

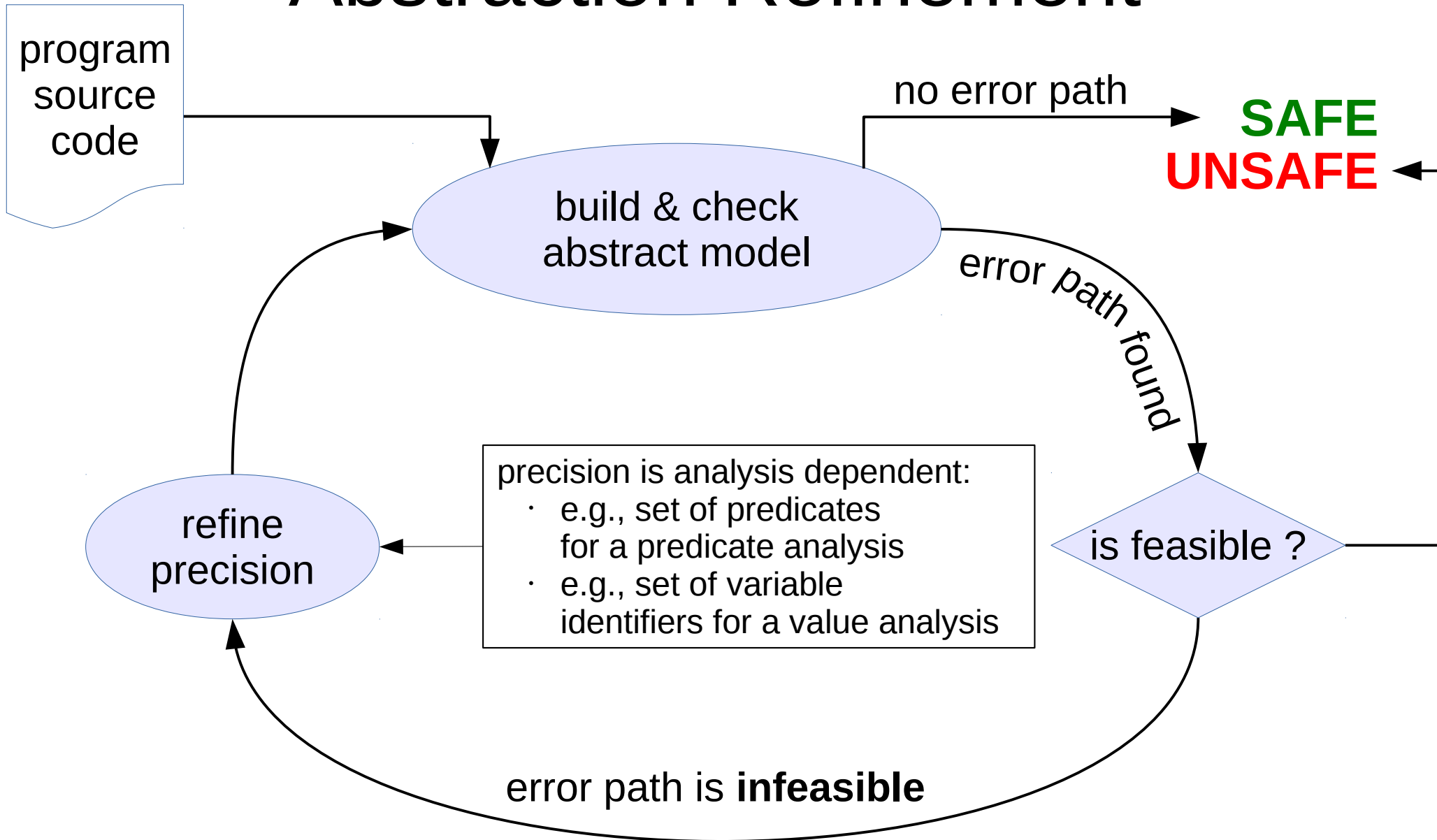
State-space explosion is prime reason for extreme resource consumption

# State-Space Explosion

```
1 #include <assert.h>
2 extern int system_call();
3
4 int main(int x) {
5     int flag = 0, ticks = 0;
6     int result;
7
8     while(1) {
9         ticks = ticks + 1;
10        result = system_call();
11
12        if(result == 0 || ticks > x) {
13            break;
14        }
15    }
16
17    if(flag > 0) {
18        assert(0);
19    }
20 }
```

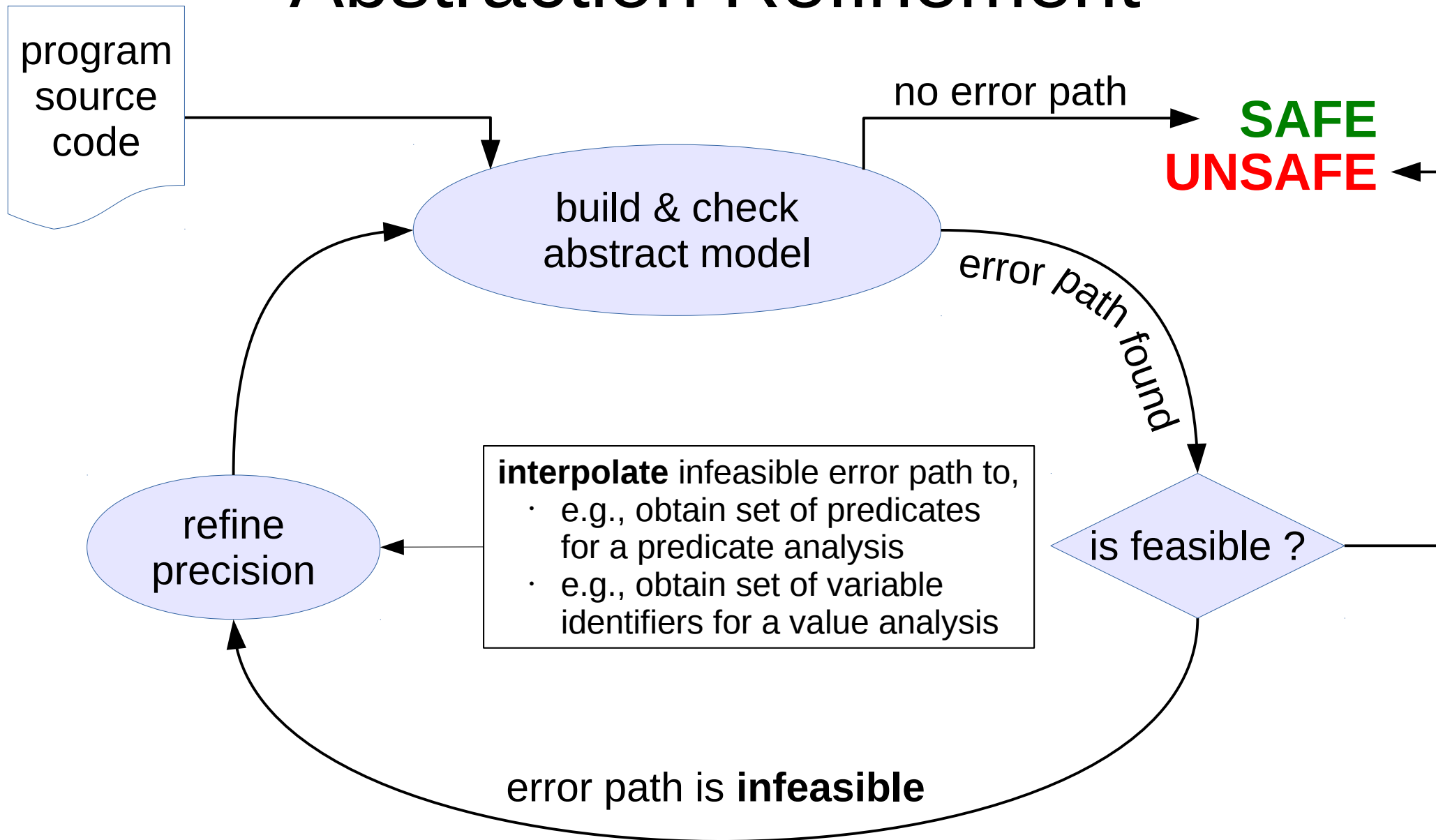


# Counterexample-Guided Abstraction Refinement



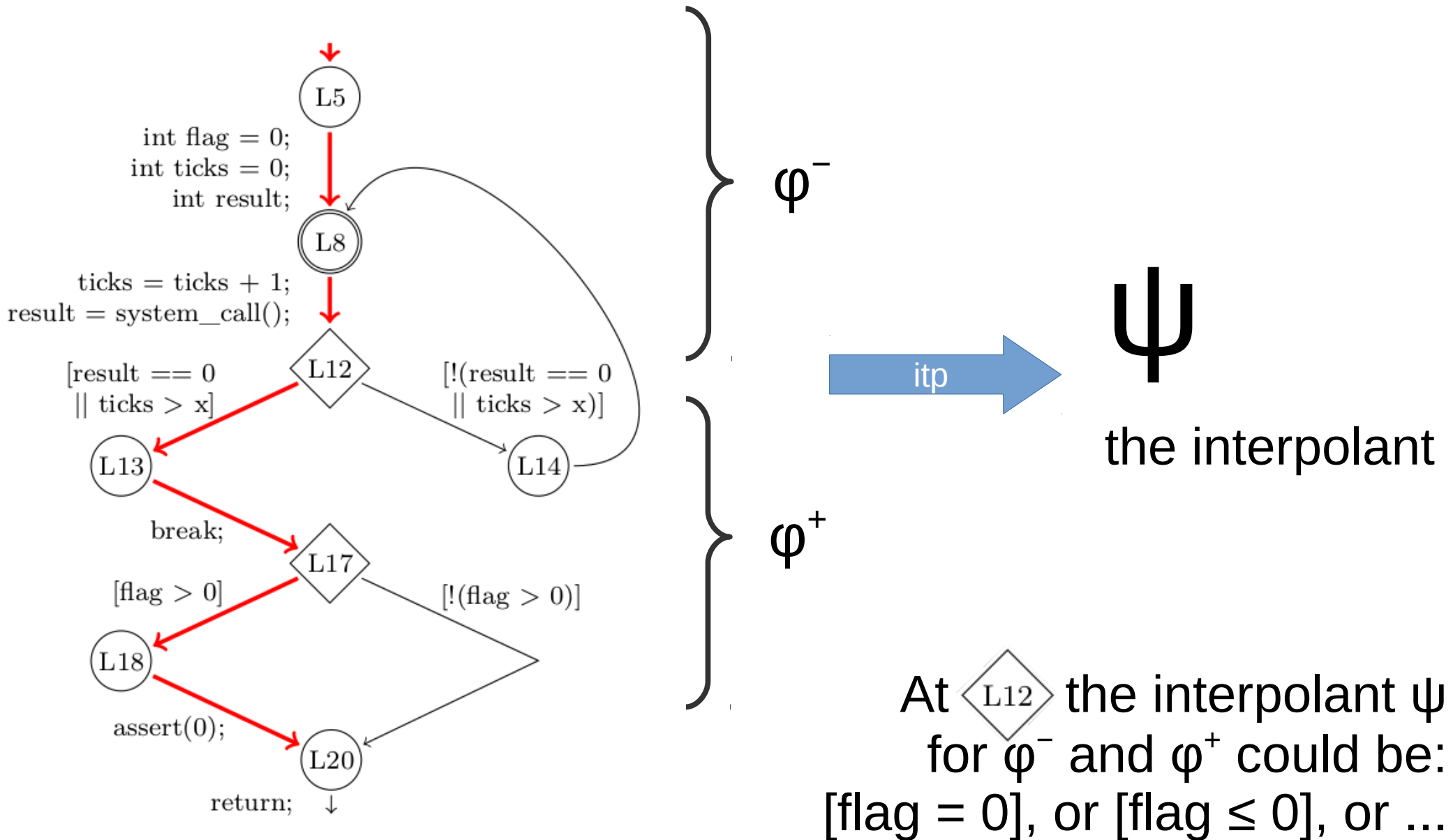


# Counterexample-Guided Abstraction Refinement



# Craig Interpolation

[Abstractions from Proofs, 2004, Henzinger, Jhala, Majumdar, McMillan]



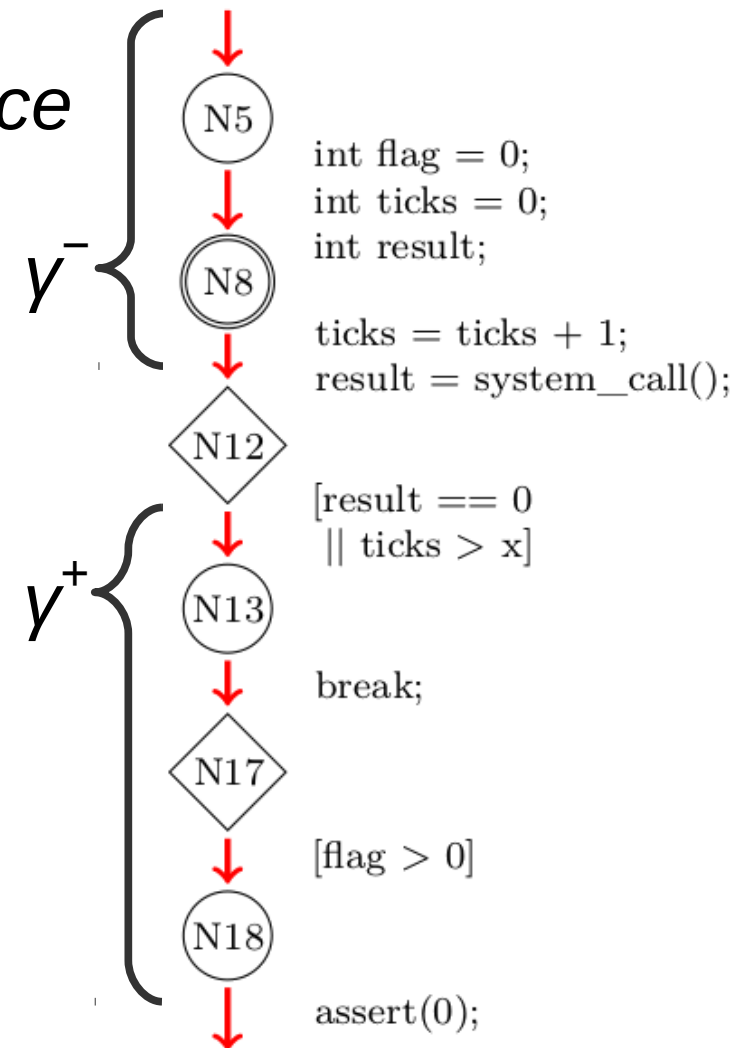
# Value Interpolation

[Explicit-State Software Model Checking Based on CEGAR and Interpolation, 2013, Beyer, Löwe]

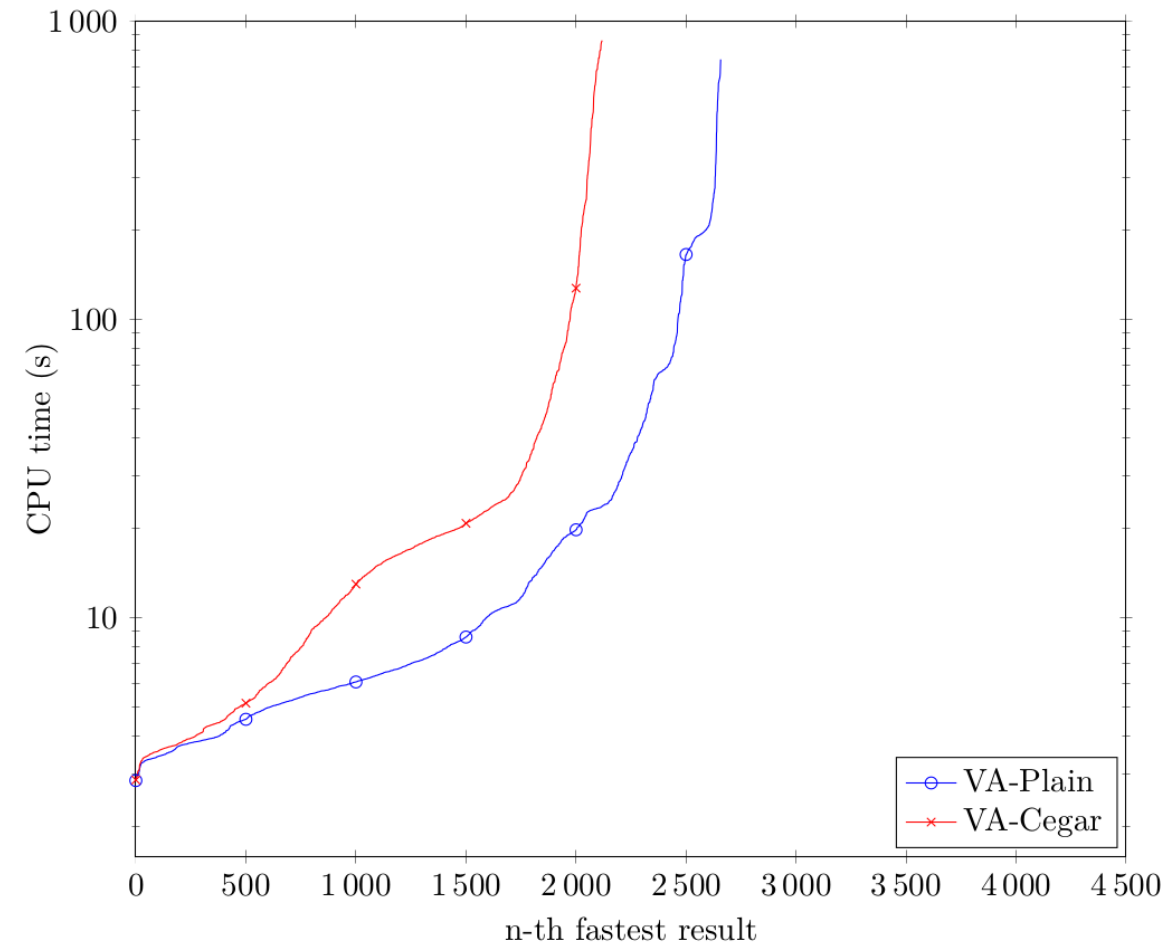
For a pair of *constraint sequences*  $\gamma^-$  and  $\gamma^+$ , such that  $\gamma^- \wedge \gamma^+$  is *contradicting*, an *interpolant*  $\psi$  is a *constraint sequence* that fulfills the following requirements:

- 1)  $\gamma^-$  implies  $\psi$
- 2)  $\psi \wedge \gamma^+$  is unsatisfiable
- 3)  $\psi$  only contains symbols that are common to both  $\gamma^-$  and  $\gamma^+$

A  $\diamond_{L12}$  the interpolant  $\psi$  for  $\gamma^-$  and  $\gamma^+$  can only be:  
[flag = 0]



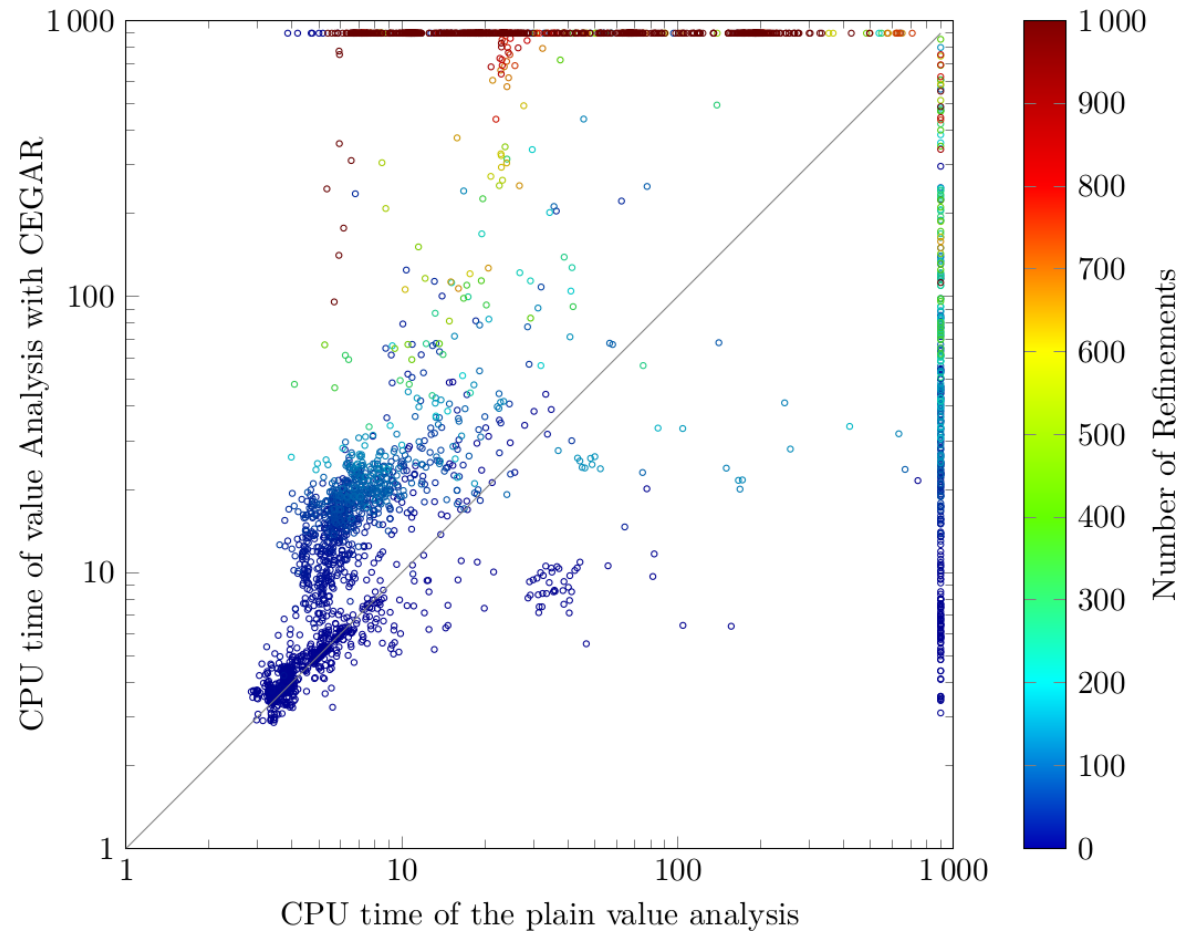
# Comparison to Plain Value Analysis



- Significant improvements in DeviceDrivers64Linux
- Significant regressions in ECA and ProductLines
- In total solves around 500 verification task less

High number of refinements is prime reason for overall regression

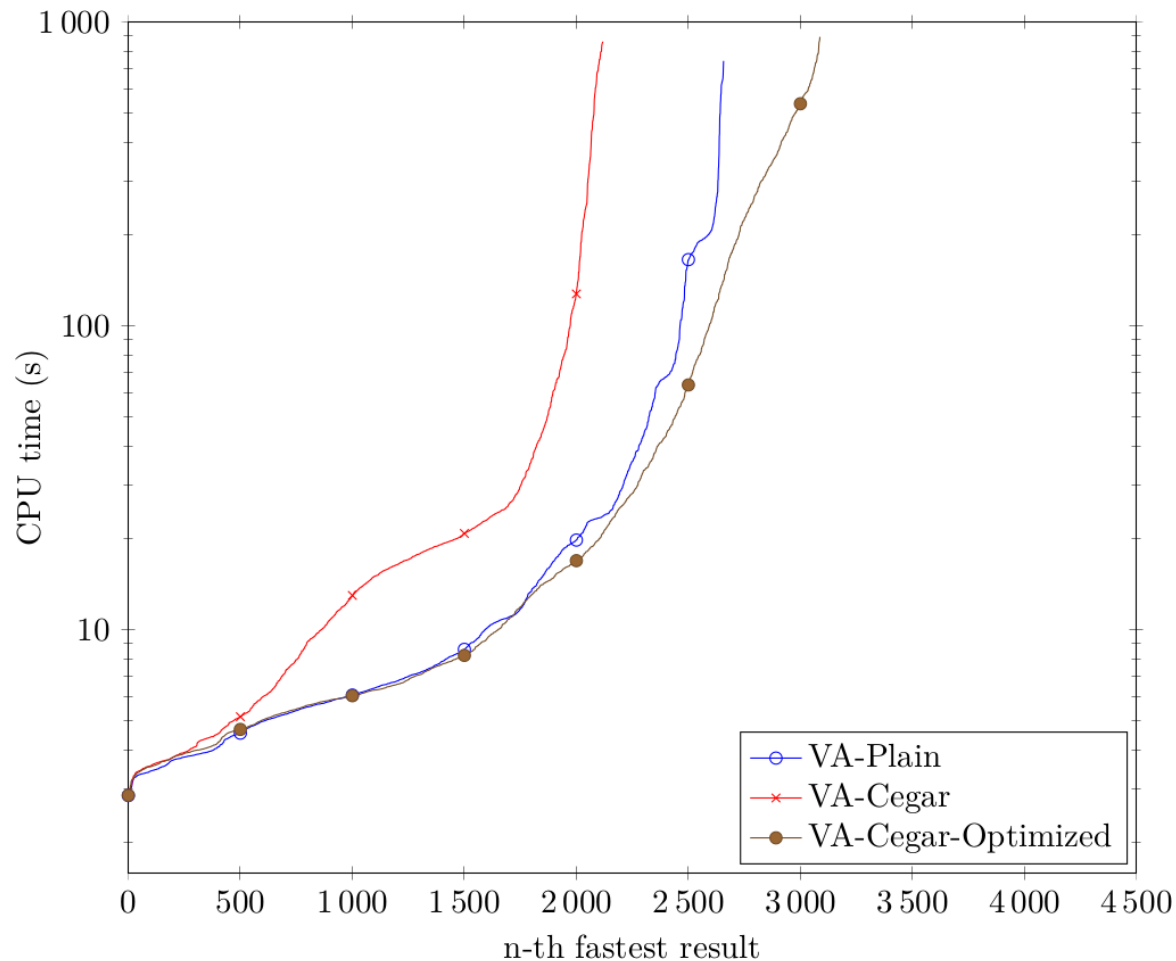
# Inspecting Number of Refinements



At least three clusters distinguishable

- Solved by both  
#refinements  $< 200$
- Solved only by VA-Cegar  
#refinements  $< 500$
- Solved only by VA-Plain  
#refinements  $> 1000$

# Reducing Time for Refinements

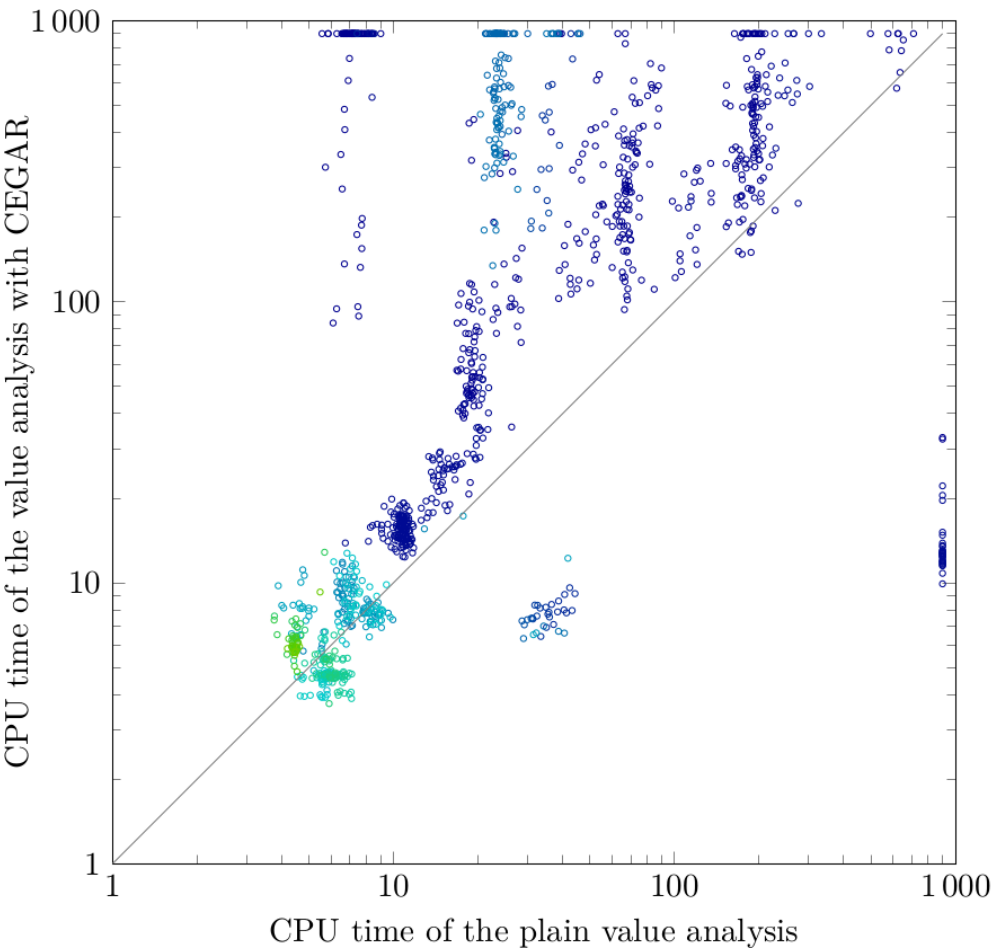


- Optimized Interpolation
  - Deepest Infeasible Suffix
  - Interpolant-Equality
- Optimized Refinement
  - “Scoped” Precision
  - Eager Restart

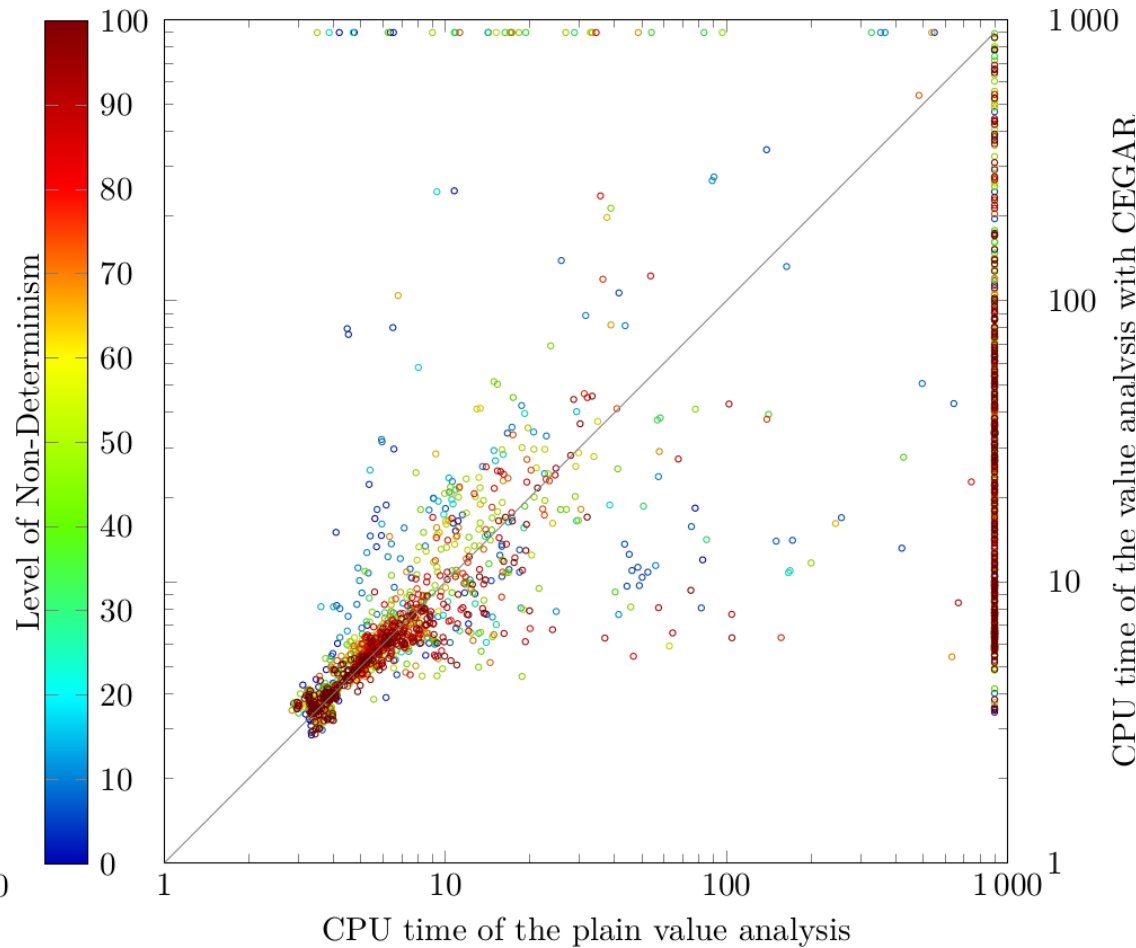
➤ CEGAR pays off, solving well over 400 tasks more

➤ Lazy abstraction is not well-suited for the Value Analysis

# Level of Non-Determinism



Low level of non-determinism:  
Use Plain Value Analysis



High level of non-determinism:  
Use Value Analysis with CEGAR

➤ Valid indicator whether to perform abstraction or not

# Versatility of Value Interpolation

- Applicable to other analyses
  - Octagon analysis
  - Symbolic execution analysis
- Enables regression verification
- Parallel composition with Predicate Analysis
- Availability of several effective analyses based on CEGAR
- Next: Techniques that may benefit **all such analyses**



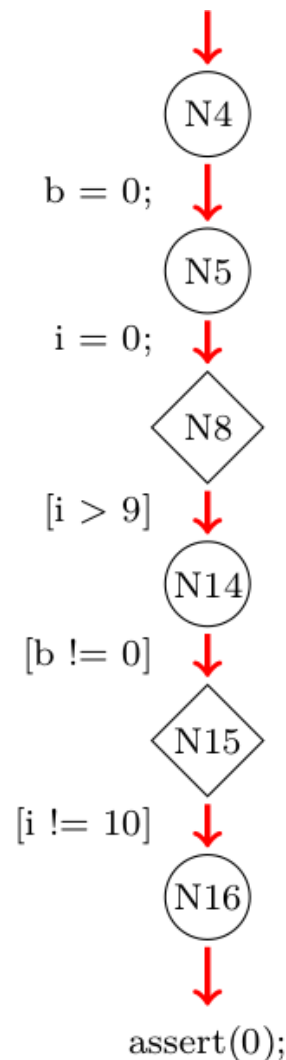
# Infeasible Sliced Prefixes and Refinement Selection

```

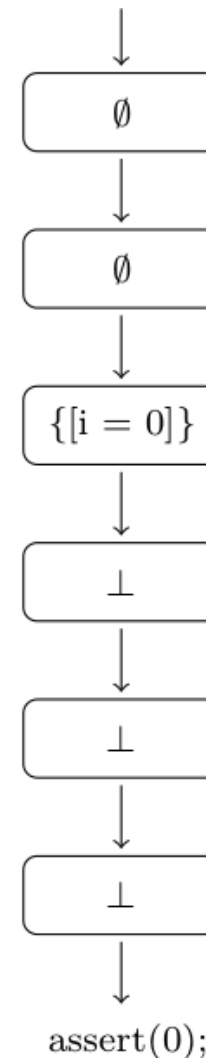
1  #include <assert.h>
2  extern int f(int x);
3  int main() {
4      int b = 0;
5      int i = 0;
6
7      while(1) {
8          if(i > 9) {
9              break;
10         }
11         f(i++);
12     }
13
14     if(b != 0) {
15         if(i != 10) {
16             assert(0);
17         }
18     }
19 }

```

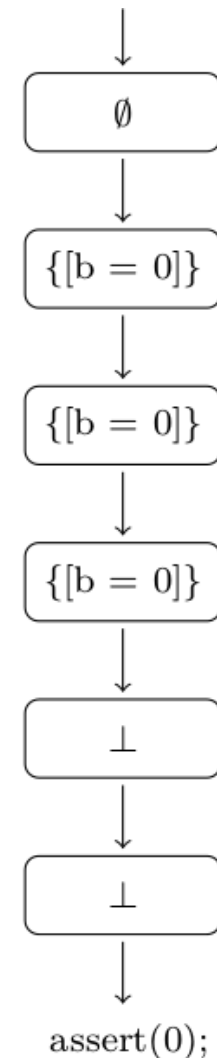
(a) verification task



(b) error path



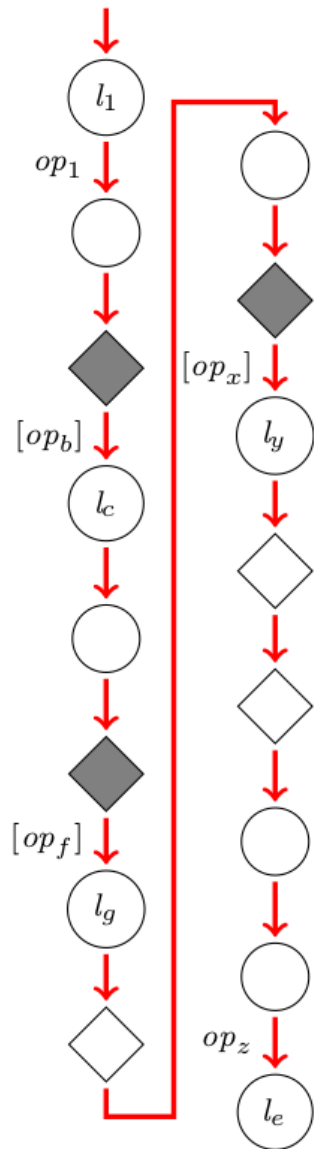
(c) bad sequence



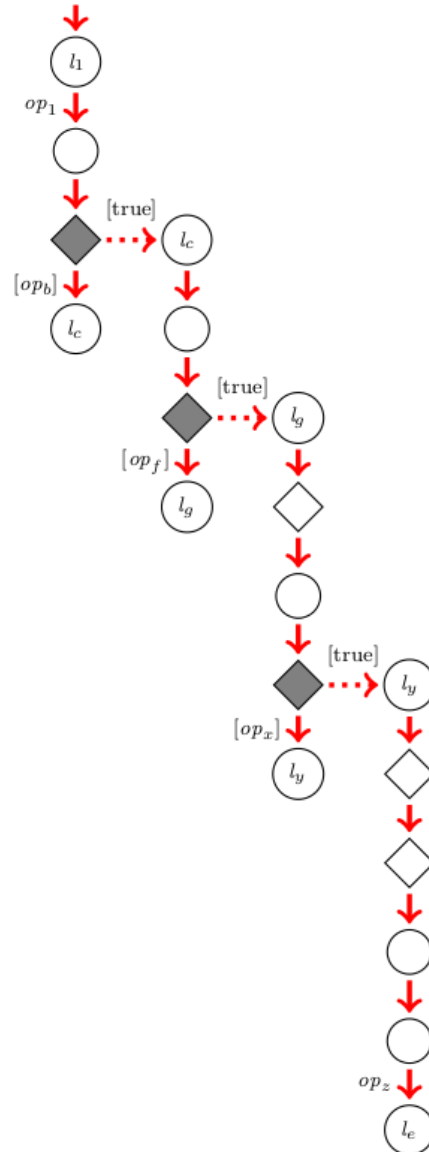
(d) good sequence

# Extraction of Infeasible Sliced Prefixes

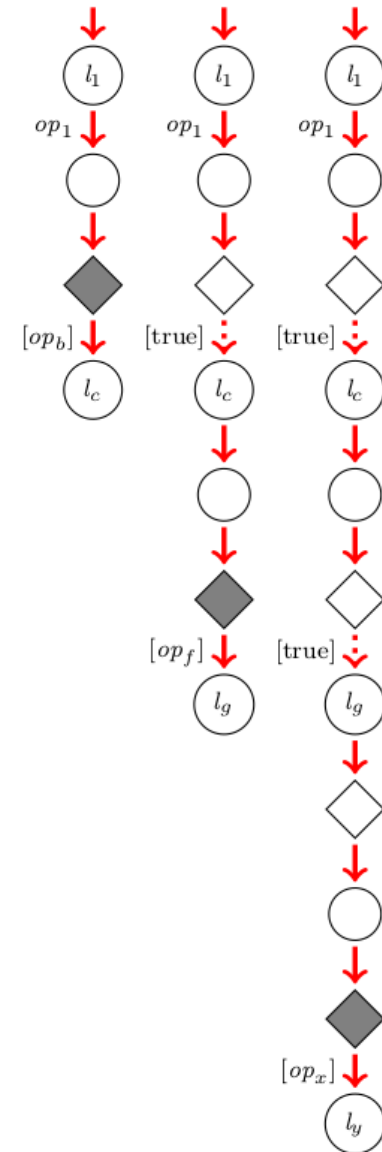
[Sliced Path Prefixes: An Effective Method to Enable Refinement Selection, 2015, Beyer, Löwe, Wendler]



(a) Infeasible error path



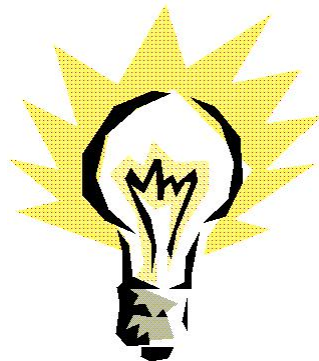
(b) Cascade of sliced prefixes



(c) Infeasible sliced prefixes

# Main Message

Any **infeasible sliced prefix  $\varphi$** ,  
that is extracted from an **infeasible error path  $\sigma$** ,  
can be used **for interpolation**  
to **exclude the original error path  $\sigma$**   
from **subsequent iterations** of CEGAR loop.



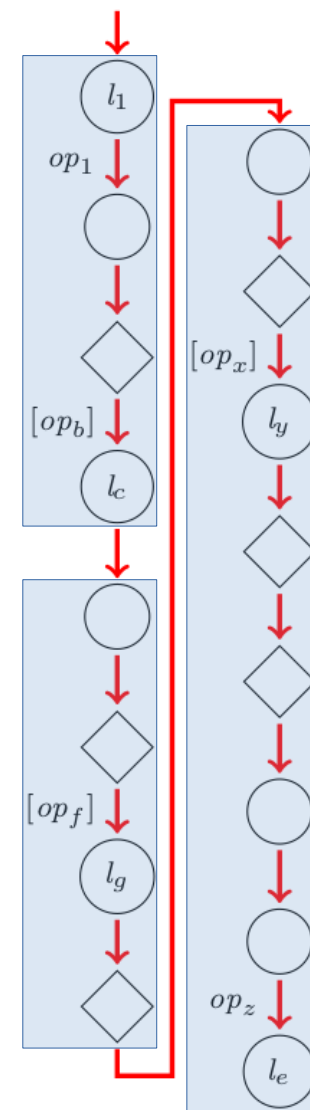
- We can use any prefix we want for interpolation !

# Sliced Prefixes - Further Applications

- Enables guided refinement selection
- Improves effectiveness and efficiency of static refinement
- Speeds up Value Interpolation significantly
- Impressive results in combination with symbolic execution
- Better control for global refinement
  - All target states at once
  - Each target state with an unique refinement
- Infeasible Sliced Prefixes for ABE?

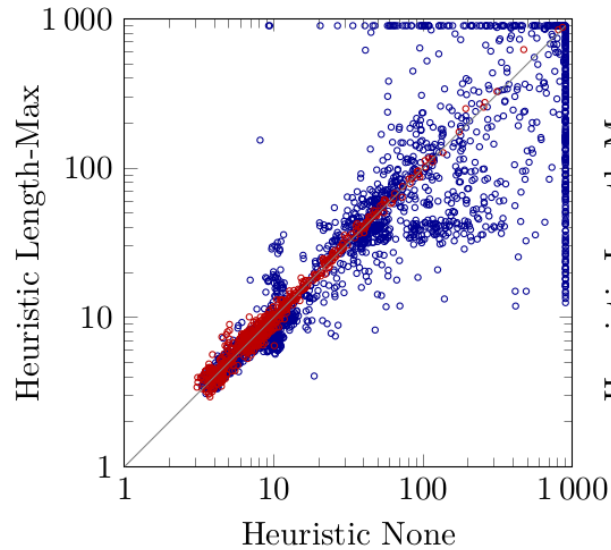
# Infeasible Sliced Prefixes for ABE?

- ABE: block size can have any size
- ABE-encoded path represent different paths
  - Simply pick one? No!
  - Simply pick all? No!
- Just think in blocks
  - SBE-encoded paths also are made of blocks
  - SBE: each block contains a single statement

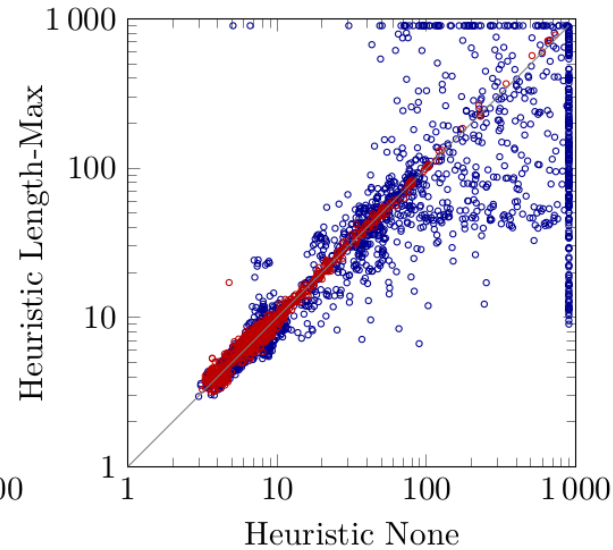


- For ABE: apply same approach as for SBE / Value Analysis

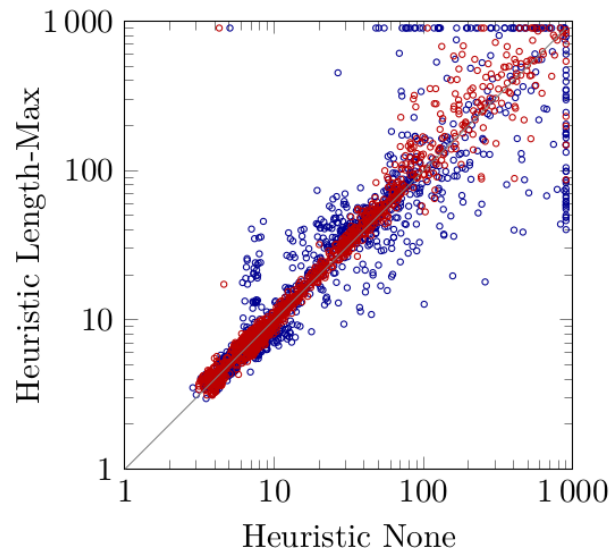
# Infeasible Sliced Prefixes for ABE



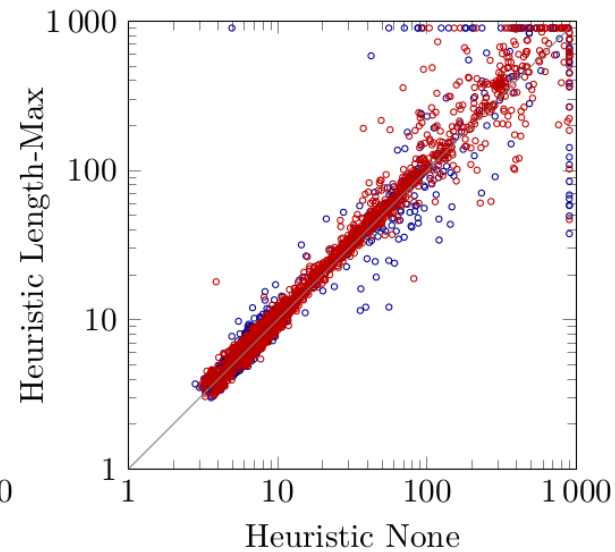
(a) None vs. Length-Max with SBE



(b) None vs. Length-Max with ABE-lj



(c) None vs. Length-Max with ABE-lf



(d) None vs. Length-Max with ABE-l

# Elimination of Infeasible Sliced Prefixes !

```
1 extern void VERIFIER_error ();
2 void VERIFIER_assert(int cond) {
3     if (!(cond)) {
4         ERROR: VERIFIER_error ();
5     }
6     return;
7 }
8
9 int main(void) {
10    unsigned int x = 1;
11    unsigned int y = 0;
12    while (y < 1024) {
13        x = 0;
14        y++;
15    }
16
17    VERIFIER_assert(x == 0);
18 }
```

(a) Source code of verification task

```
1 main();
-----
2 x = 1;
3 y = 0;
-----
4 [y < 1024]
5 x = 0;
6 y = y + 1;
-----
8 [y < 1024]
9 x = 0;
10 y = y + 1;
-----
12 [!(y < 1024)]
13 VERIFIER_assert((x == 0)
14 ? cond = 1
15 : cond = 0);
-----
15 [cond == 0]
16 VERIFIER_error ();
```

(b) Error path over two loop iteration

Verification task `const_true-unreach-call1.c` from the official SVCOMP'16 repository, and a possible infeasible error path when analyzing the task with ABE-If

# Elimination of Infeasible Sliced Prefixes !

```
1 extern void VERIFIER_error();
2 void VERIFIER_assert(int cond) {
3     if (!(cond)) {
4         ERROR: VERIFIER_error();
5     }
6     return;
7 }
8
9 int main(void) {
10    unsigned int x = 1;
11    unsigned int y = 0;
12    while (y < 1024) {
13        x = 0;
14        y++;
15    }
16
17    VERIFIER_assert(x == 0);
18 }
```

(a) Source code of verification task

```
1 main();
-----
2 x = 1;
3 y = 0;
-----
4 [y < 1024]
5 x = 0;
6 y = y + 1;
-----
8 [y < 1024]
9 x = 0;
10 y = y + 1;
-----
12 [!(y < 1024)]
13 VERIFIER_assert((x == 0)
14 ? cond = 1
15 : cond = 0);
-----
15 [cond == 0]
16 VERIFIER_error();
```

$\Psi: [y = 2]$

(b) Error path over two loop iteration

Verification task `const_true-unreach-call1.c` from the official SVCOMP'16 repository, and a possible infeasible error path when analyzing the task with ABE-If



# Elimination of Infeasible Sliced Prefixes !

```
1 extern void VERIFIER_error();
2 void VERIFIER_assert(int cond) {
3     if (!(cond)) {
4         ERROR: VERIFIER_error();
5     }
6     return;
7 }
8
9 int main(void) {
10    unsigned int x = 1;
11    unsigned int y = 0;
12    while (y < 1024) {
13        x = 0;
14        y++;
15    }
16
17    VERIFIER_assert(x == 0);
18 }
```

(a) Source code of verification task

```
1 main();
-----
2 x = 1;
3 y = 0;
-----
4 [y < 1024]
5 x = 0;
6 y = y + 1;
-----
8 [y < 1024]
9 x = 0;
10 y = y + 1;
-----
12 !(y < 1024)]
13 VERIFIER_assert((x == 0)
14 ? cond == 1
15 : cond = 0);
-----
15 [cond == 0]
16 VERIFIER_error();
```

(b) Error path over two loop iteration

- For ABE: this approach is also not perfect
- Any other ideas?

# Quite good for LDV

Tool	CPAchecker 1.6.1-svn 23191M			
Date of execution	2016-09-22 23:40:40 CEST			
Run set	original		refSel-abe-lj	
Options	-noout -heap 25000M -ldv		-noout -heap 25000M -ldv -setprop cpa.value.refinement.prefixPreference=DOMAIN_MIN,LENGTH_MAX -setprop cpa.value.refinement.restart=ROOT -setprop cpa.value.refinement.addAssumptionsToCex=false -setprop cpa.predicate.abstraction.computation=BOOLEAN -setprop cpa.predicate.blk.alwaysAtJoin=true -setprop cpa.predicate.blk.alwaysAtFunctions=false -setprop cpa.predicate.blk.alwaysAtLoops=true -setprop cpa.predicate.refinement.performInitialStaticRefinement=false -setprop cpa.predicate.refinement.prefixPreference=DOMAIN_MIN,LENGTH_MAX -setprop cpa.predicate.refinement.restartAfterRefinements=1 -setprop cpa.predicate.memoryAllocationsAlwaysSucceed=true -setprop cpa.predicate.precision.sharing=SCOPE -setprop cegar.refiner=cpa.value.refiner.ValueAnalysisDelegatingRefiner -setprop cegar.useRefinementSelection=true -setprop cegar.domainScoreThreshold=4	
test/programs/benchmarks/	status	cputime (s)	status	cputime (s)
ldv-linux-4.2-rc1/linux-4.2-rc1.tar.xz-43_2a-drivers--tty--serial--jsm.cil.out.c	timeout	1000	true	48.9
ldv-linux-4.2-rc1/linux-4.2-rc1.tar.xz-43_2a-drivers--tty--synclink_gtout.c	timeout	929	true	94.3
ldv-linux-4.2-rc1/linux-4.2-rc1.tar.xz-43_2a-drivers--tty--synclinkmp.ut.c	timeout	916	true	81.1
ldv-linux-4.2-rc1/linux-4.2-rc1.tar.xz-43_2a-drivers--usb--host--ehci-il.out.c	timeout	921	true	158
ldv-linux-4.2-rc1/linux-4.2-rc1.tar.xz-43_2a-drivers--usb--host--fotg2l.cil.out.c	timeout	1000	true	132
ldv-linux-4.2-rc1/linux-4.2-rc1.tar.xz-43_2a-drivers--usb--host--fusbhll.cil.out.c	timeout	1000	true	139
ldv-linux-4.2-rc1/linux-4.2-rc1.tar.xz-43_2a-drivers--usb--host--ohci-il.out.c	timeout	1000	true	141
ldv-linux-4.2-rc1/linux-4.2-rc1.tar.xz-43_2a-drivers--usb--host--oxu21ll.cil.out.c	timeout	1000	true	471
ldv-linux-4.2-rc1/linux-4.2-rc1.tar.xz-43_2a-drivers--usb--host--r8a66ll.cil.out.c	timeout	916	true	101
ldv-linux-4.2-rc1/linux-4.2-rc1.tar.xz-43_2a-drivers--usb--serial--digch-call.cil.out.c	timeout	924	true	157
ldv-linux-4.2-rc1/linux-4.2-rc1.tar.xz-43_2a-drivers--usb--serial--moscil.out.c	timeout	1000	true	46.8
ldv-linux-4.2-rc1/linux-4.2-rc1.tar.xz-43_2a-drivers--usb--storage--ua.out.c	timeout	1000	true	311
ldv-linux-4.2-rc1/linux-4.2-rc1.tar.xz-43_2a-drivers--video--fbdev--ath-call.cil.out.c	timeout	907	true	140
ldv-linux-4.2-rc1/linux-4.2-rc1.tar.xz-43_2a-drivers--video--fbdev--viall.cil.out.c	timeout	922	true	82.4
ldv-linux-4.2-rc1/linux-4.2-rc1.tar.xz-43_2a-drivers--xen--xen-pcibackach-call.cil.out.c	timeout	1000	true	88.5
ldv-challenges/linux-3.8-rc1-32_7a-drivers--md--md-mod.ko-ldv_main0_see-unreach-call.cil.out.c	timeout	912	true	405
test/programs/benchmarks/	status	cputime (s)	status	cputime (s)
total tasks	267	239000	267	89000
correct results	26	8360	236	62600
score (267 tasks, max score: 496)	-19	-	411	-
Run set	original		refSel-abe-lj	

Questions ?